

BucketSort and Lowerbounds for Sorting Reset Progress

Reveal Solutions

1 Comparison Based Sorting Lowerbound

Assume you have a function called 3-sort that takes as input an array of size 3 of comparable objects and returns them in sorted order. You want to sort an array of size $n \geq 3$ objects only using calls to 3-sort, How many function calls of 3-sort are required to sort an array of size n ?

- ☐ $\Omega(\log(n))$
- ☐ $\Omega(\sqrt{n})$
- ☐ $\Omega(n)$
- ☒ $\Omega(n \log n)$

Correct

Is it possible to implement the following algorithms or data structures in real life?

A data structure that you can insert comparable objects in $O(1)$ operations, remove them in $O(1)$ operations, and make function calls to a function that returns the smallest object in the data structure in $O(1)$?

- ☐ Possible
- ☒ Impossible

Correct

An algorithm that runs in $O(n)$ and takes an array A of size n of comparable objects, i , and j ($i < j$) as inputs and returns all the elements that are greater than the i th element in A and less than the j th element in A ?

- ☒ Possible
- ☐ Impossible

Correct

Which algorithm would be a good choice to use for the last part?

- ☒ k-select
- ☐ Radix Sort
- ☐ QuickSort
- ☐ MergeSort

Correct

An algorithm that runs in $\Theta(n)$ and takes an array A of size n of comparable objects and partitions A into $\frac{n}{\log(n)}$ groups of size $\log(n)$ where for every $i < j$ members of group i are smaller than or equal to members of group j .

- ☐ Possible
- ☒ Impossible

Correct

2 Radix Sort and Counting Sort

Assume you have an array A of size n with positive integer element with all elements in range of $[1, n^3]$. What is the runtime of Counting sort run on A?

- ☐ $\Theta(n)$
- ☐ $\Theta(n \log n)$
- ☐ $\Theta(n^2)$
- ☒ $\Theta(n^3)$

Correct

What is the runtime of Radix sort, base 10, run on A?

- ☐ $\Theta(n)$
- ☒ $\Theta(n \log n)$
- ☐ $\Theta(n^2)$
- ☐ $\Theta(n^3)$

Correct

Which base for Radix sort will result in the fastest Radix sort algorithm to sort A with?

- ☐ 2
- ☐ 10
- ☒ n
- ☐ n^2

Correct